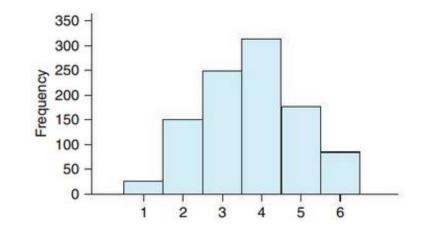


SUMMARIES FOR DISTRIBUTIONS

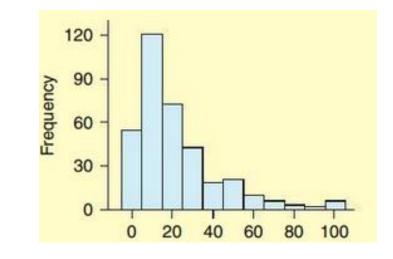
Symmetric Distributions

- Bell shaped
- The mean is a good representation for the "typical value"
- Mean = Median
- Majority of observations are less than one standard deviation from the mean.

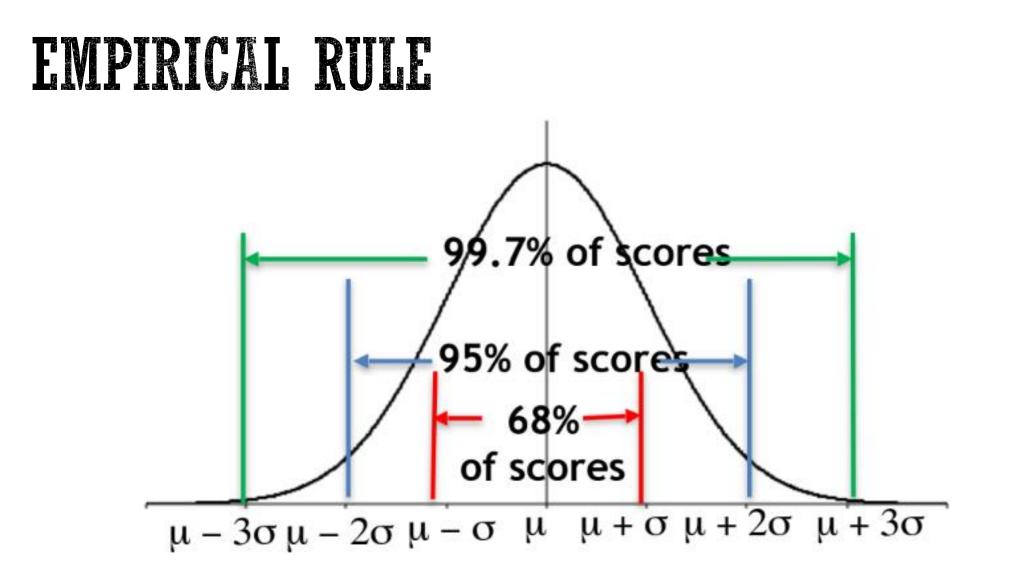


Skewed Distributions

- Higher on one end
- The median represents a "typical value" in a skewed distribution
- Skewed Left: Mean < Median</p>
- Skewed Right: Mean > Median









Z-SCORES

- Z-Scores measure how many standard deviations away an observation is from the mean.
 - Positive Z-Score \rightarrow Observed value is greater than the mean
 - Negative Z-Score \rightarrow Observed value is less than the mean

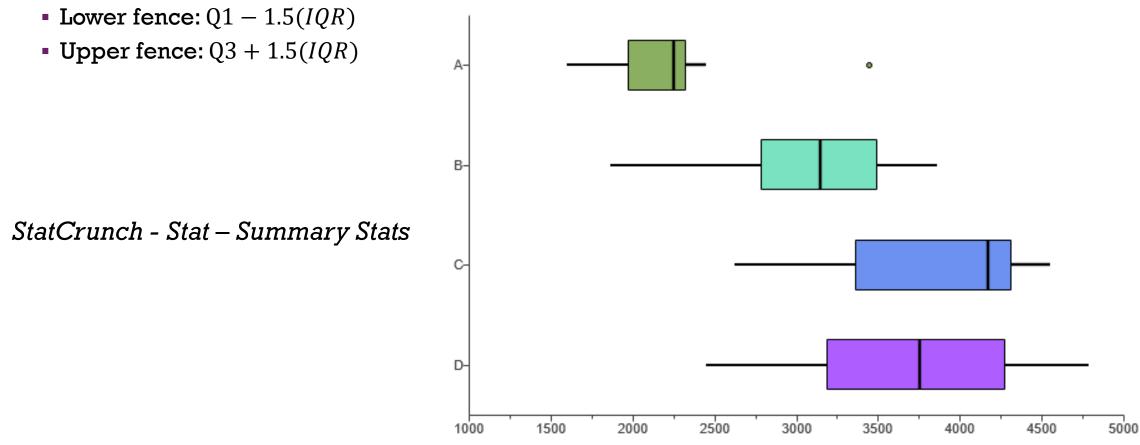
 $z = \frac{Observed Value - Mean}{Standard Deviation}$

Finding Mean and Standard Deviation: StatCrunch – Stat – Summary Stats



BOXPLOTS

- 5 number Summary: Minimum, Q1, Median, Q3, Maximum
- Potential Outliers are numbers outside the "fences":



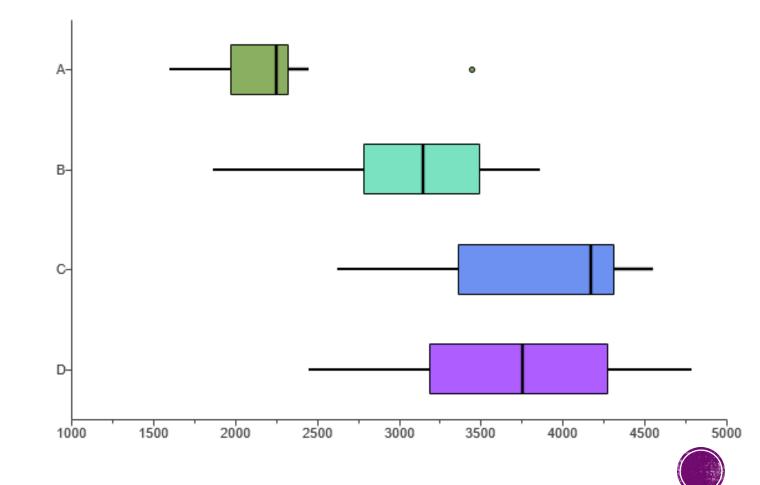
EXAMPLE: ANALYZE BOXPLOTS

Which boxplot shows the most variation?

Boxplot D

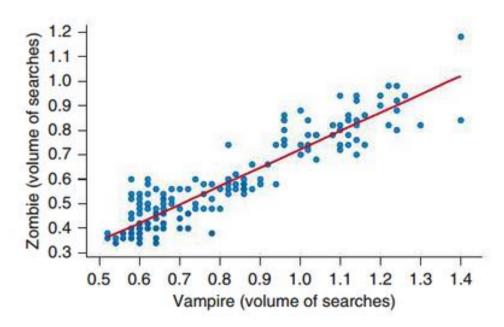
Which boxplot shows the least variation?

Boxplot A



REGRESSION ANALYSIS

- Correlation Coefficient (r): Always between -1 and 1
 - A strong correlation is closer to -1 or 1
 - A weak correlation is closer to 0



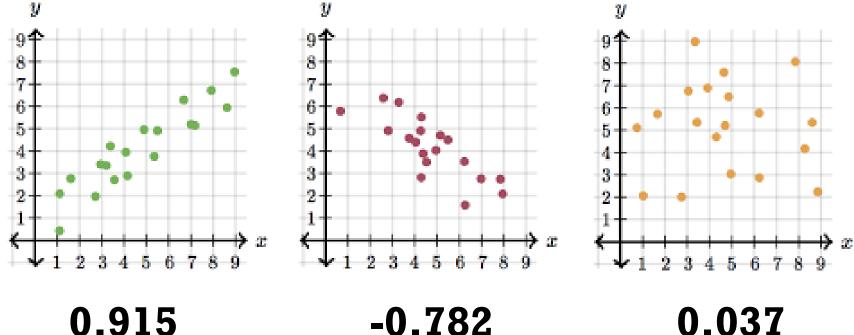
- Regression Line (also Line of Best Fit or Least Squares): For making predictions about future observed values
 - x explanatory, predictor, independent
 - y response, predicted, dependent

StatCrunch – Stat – Regression – Simple Linear – Select x and y



EXAMPLE: MATCH SCATTERPLOTS TO CALCULATED CORRELATIONS

• Three scatterplots are shown below. The calculated correlations are 0.915, -0.782, and 0.037. Determine which correlation goes with which scatterplot.

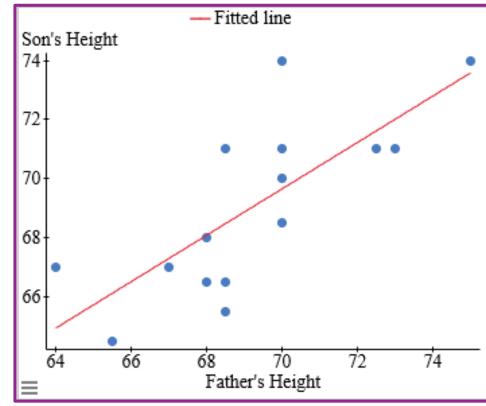




0.915

-0.782

 The accompanying table shows some data from a sample of heights of fathers and their sons. The scatterplot suggests a linear trend.



Father	Son
75	74
72.5	71
73	71
70	74
70	68.5
70	70
68	68
68	66.5
70	71
68.5	66.5
68.5	65.5
68.5	71
67	67
65.5	64.5
64	67

a. Find and report the regression equation for predicting the son's height from the father's height.

StatCrunch - Stat – Regression – Simple Linear Choose x and y variables

Son's Height=14.59 + 0.79 Father's Height

Simple linear regression results: Dependent Variable: Son's Height Independent Variable: Father's Height Son's Height = 14.586898 + 0.78641938 Father's Height Sample size: 15 R (correlation coefficient) = 0.75396424 R-sq = 0.56846207 Estimate of error standard deviation: 2.0060827

Parameter estimates:

Parameter	Estimate	Std. Err.	Alternative	DF	T-Stat	P-value
Intercept	14.586898	13.167181	≠ 0	13	1.1078224	0.288
Slope	0.78641938	0.19003836	≠ 0	13	4.1382139	0.0012

Father

75

73

72.5

Son

74

71

71

Analysis of variance table for regression model:

Source	DF	SS	MS	F-stat	P-value
Model	1	68.916552	68.916552	17.124815	0.0012
Error	13	52.316781	4.0243678		
Total	14	121.23333			

b. Interpret the slope in the context of the problem.

Son's Height=14.59 + 0.79 Father's Height

For every additional inch on the Father's height, on average, the Son's height goes up by 0.79 inches.

4 1 1 4 8.5 0 8
1 4 8.5 0
4 8.5 0
8.5 0
0
8
6.5
1
6.5
5.5
1
7
4.5
5

c. Using the regression line, predict the height of a son whose father is 74 inches tall.

Son's Height=14.59 + 0.79 Father's Height Son's Height=14.59 + 0.79 (74)

We predict the son will be 72.78 inches tall.

Note: Don't extrapolate!

Don't make predictions beyond the range of the observed data, because we are not sure that the linear trend will continue beyond the range of the data.

	Father	Son
	75	74
	72.5	71
r	73	71
•	70	74
	70	68.5
	70	70
	68	68
	68	66.5
	70	71
	68.5	66.5
	68.5	65.5
	68.5	71
	67	67
	65.5	64.5
	64	67

PROBABILITY

Theoretical Probability

- Long run relative frequencies what would occur after infinitely many repetitions
 - Rules:

 $P(x) = \frac{Number of outcomes in x}{Number of outcomes possible}$ $0 \le P(x) \le 1$

Empirical Probability

- Relative frequencies based on an experiment or on observations of a real life process
 - The Law of Large Numbers: The larger the number of repetitions, the closer the empirical probability will be to the theoretical probability



EXAMPLE: PROBABILITY

A person was trying to figure out the probability of getting two heads when flipping two coins. He flipped two coins 20 times, and in 4 of these 20 times, both coins landed heads. On the basis of this outcome, he claims that the probability of two heads is 4/20, or 20%.

Is this an example of an empirical probability or a theoretical probability? Explain.

This is an example of empirical probability because it is based on an experiment.



		Female	Male	A11
	No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185
	Yes	596	404	1000
	A11	726	551	1277

a. What is the probability that the person from the table is male?

$$\frac{551}{1277} = 0.431$$



		Female	Male	A11
	No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185
	Yes	596	404	1000
	A11	726	551	1277

b. What is the probability that the person said Yes?

 $\frac{1000}{1277} = 0.783$



		Female	Male	A11
	No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185
	Yes	596	404	1000
	A11	726	551	1277

c. Are the event being male and the event saying Yes mutually exclusive? Why or why not?

The events are not mutually exclusive because a person chosen could be male and say yes.



		Female	Male	A11
	No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185
	Yes	596	404	1000
	A11	726	551	1277

d. What is the probability that a person is male and said Yes?

$$\frac{404}{1277} = 0.316$$



		Female	Male	A11
	No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185
	Yes	596	404	1000
	A11	726	551	1277

e. What is the probability that a person is male or said Yes?

To find the probability that a person is male or said yes, why should you subtract the probability that a person is male and said Yes from the sum as shown below? *P*(male or Yes)=*P*(male)+*P*(Yes)-*P*(male and Yes)

$$\frac{551}{1277} + \frac{1000}{1277} - \frac{404}{1277} = \mathbf{0.898}$$



			Female	Male	A11
		No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185	
	Yes	596	404	1000	
		A11	726	551	1277

f. What is the probability that a randomly chosen person was male given that the person said Yes. In other words, what percentage of the people who said Yes were male?

$$\frac{404}{1000} = 0.404$$

= 40.4%



		Female	Male	A11
	No	41	51	92
EXAMPLE: PROBABILITY	Unsure	89	96	185
	Yes	596	404	1000
	A11	726	551	1277

g. Find the probability that a randomly chosen person who reported being Unsure was female. In other words, what percentage of the people who were Unsure were female?

$$\frac{89}{185} = 0.481$$

= 48.1%

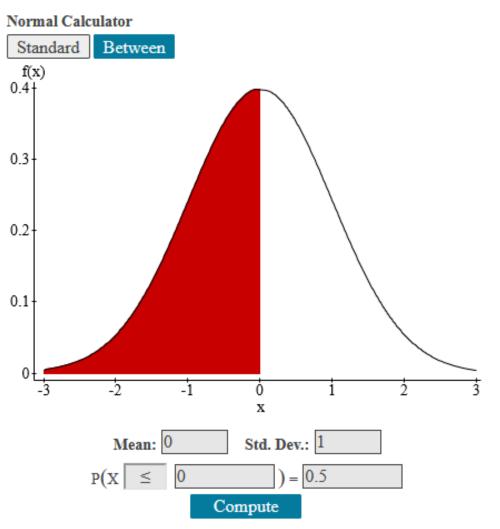


NORMAL DISTRIBUTION

- Finding probabilities by finding the area under the Normal Curve.
- Percentiles: Area based on percentage used to work backwards
 - 90th Percentile means 90% of the data is below that value or

90% of the area under the Normal curve is to its left.

StatCrunch – Stat – Calculators – Normal





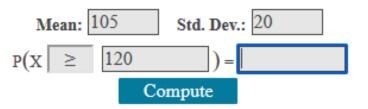
Assume that adults have IQ scores that are Normally distributed with a mean of $\mu = 105$ and a standard deviation $\sigma = 20$. Find the probability that a randomly selected adult has an IQ of 120 or above.

StatCrunch – Stat – Calculators – Normal

Fill in mean, standard deviation, and score.



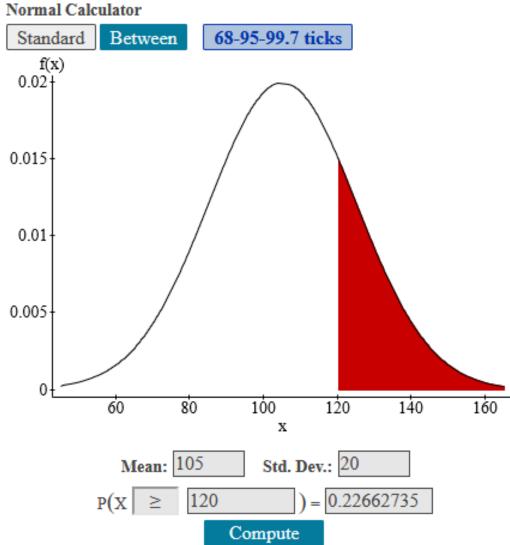
Press Enter or Compute to update.



Assume that adults have IQ scores that are Normally distributed with a mean of $\mu = 105$ and a standard deviation $\sigma = 20$. Find the probability that a randomly selected adult has an IQ of 120 or above.

StatCrunch – Stat – Calculators – Normal

The probability that a randomly selected adult has an IQ of 120 or more is 0.227.

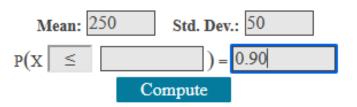


The average birth weight of elephants is 250 pounds. Assume that the distribution of birth weights is Normal with a standard deviation of 50 pounds. Find the birth weight of elephants at the 90th percentile

StatCrunch – Stat – Calculator – Normal Fill in mean, standard deviation, and probability.



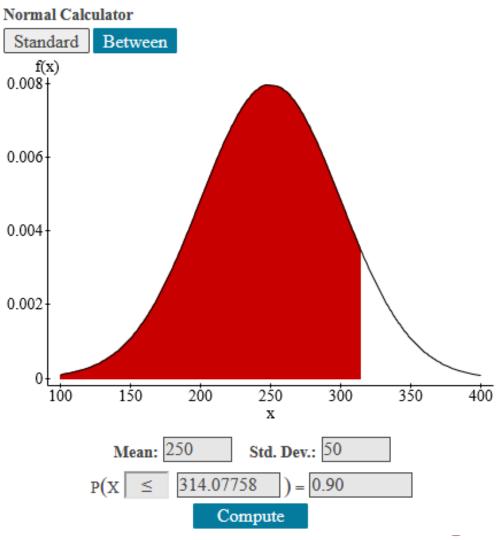
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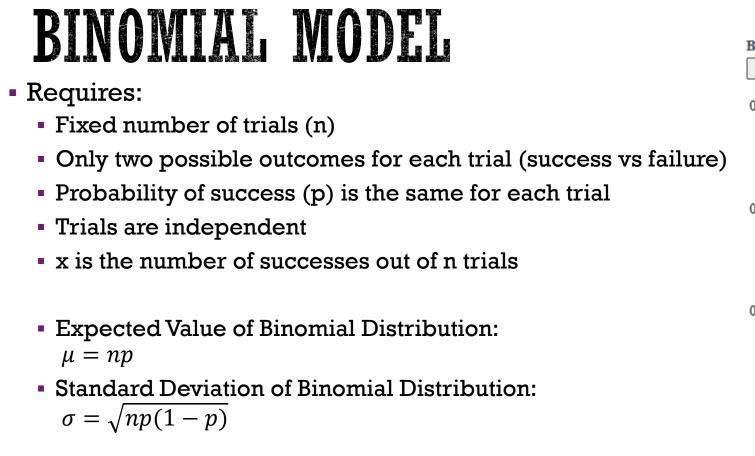


The average birth weight of elephants is 250 pounds. Assume that the distribution of birth weights is Normal with a standard deviation of 50 pounds. Find the birth weight of elephants at the 90th percentile

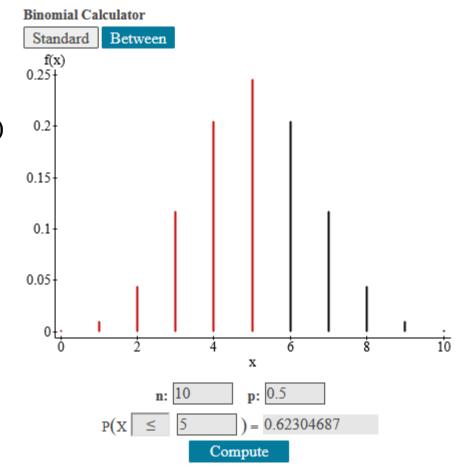
StatCrunch – Stat – Calculator – Normal Fill in mean, standard deviation, and probability.

The birth weight of elephants at the 90th percentile is 314 pounds.





StatCrunch – Stat – Calculators – Binomial





BINOMIAL MODEL

- Because the binomial probability distribution models probability of discrete random variables, we have to pay attention to the wording!
 - "Exactly 6" $\rightarrow P(X = 6)$
 - "More than 6" $\rightarrow P(X > 6)$
 - "At least 6" $\rightarrow P(X \ge 6)$
 - "6 or more" $\rightarrow P(X \ge 6)$
 - "Less than 6" $\rightarrow P(X < 6)$
 - "Fewer than 6" $\rightarrow P(X < 6)$
 - "At most 6" $\rightarrow P(X \le 6)$



EXAMPLE: BINOMIAL MODEL

A recent poll indicated that about 74% of U.S. households had access to a high-speed Internet connection.

a. Suppose 100 households were randomly selected from the United States. How many of the households would you expect to have access to a high-speed Internet connection?

Expected value = $np \rightarrow 100(0.74) = 74$

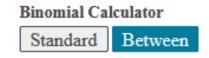
You would expect 74 households to have access to high-speed internet connection.



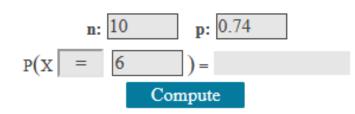
A recent poll indicated that about 74% of U.S. households had access to a high-speed Internet connection.

b. If 10 households are selected randomly, what is the probability that exactly 6 have high-speed access?

StatCrunch – Stat – Calculators – Binomial



Press Enter or Compute to update.



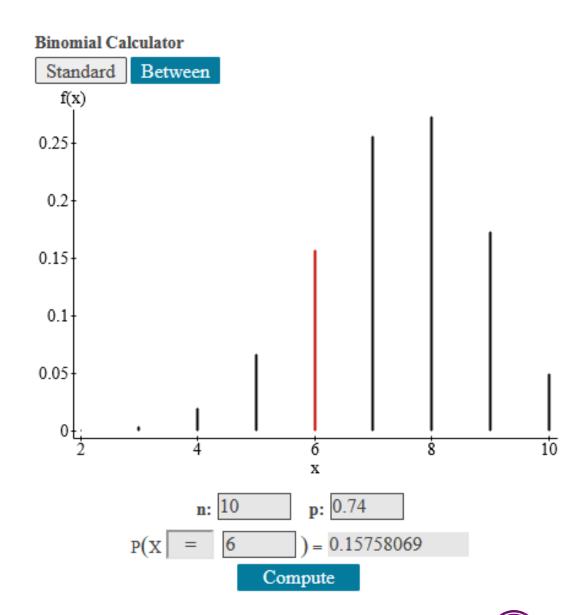


A recent poll indicated that about 74% of U.S. households had access to a high-speed Internet connection.

b. If 10 households are selected randomly, what is the probability that exactly 6 have high-speed access?

StatCrunch – Stat – Calculators – Binomial

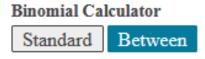
The probability that exactly 6 households have high-speed access is 0.158



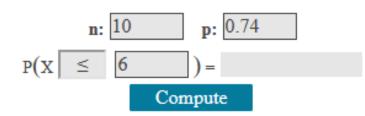
A recent poll indicated that about 74% of U.S. households had access to a high-speed Internet connection.

c. If 10 households are selected randomly, what is the probability that 6 or fewer have high-speed access?

StatCrunch – Stat – Calculators – Binomial



Press Enter or Compute to update.



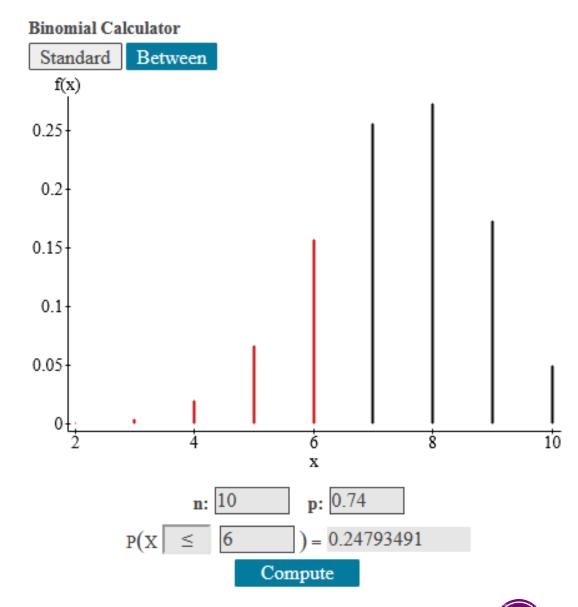


A recent poll indicated that about 74% of U.S. households had access to a high-speed Internet connection.

c. If 10 households are selected randomly, what is the probability that 6 or fewer have high-speed access?

StatCrunch – Stat – Calculators – Binomial

The probability that exactly 6 or fewer households have high-speed access is 0.248





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